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A MIXED-MODE BENDING APPARATUS FOR DELAMINATION TESTING

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SUMMARY

A mixed-mode delamination test procedure was developed combining double cantilever beam (DCB) mode I loading and end notch flexure (ENF) mode II loading on a split unidirectional laminate. By loading the specimen with a lever, a single applied load simultaneously produces mode I and mode II bending loads on the specimen. This mixed-mode bending (MMB) test was analyzed using both finite element procedures and beam theory to calculate the mode I and mode II components of strain energy release rate, G_I and G_{II} , respectively. The analyses showed that a wide range of G_I/G_{II} ratios could be produced by varying the applied load position on the loading lever. As the delamination extended, the G_I/G_{II} ratios varied by less than five percent. The simple beam theory equations were modified to account for the elastic interaction between the two arms of the specimen and to account for shear deformations. The resulting equations agreed closely with the finite element results and provide a basis for selection of G_I/G_{II} test ratios and a basis for computing the mode I and mode II components of measured delamination toughness. The MMB specimen analysis and test procedures were demonstrated using AS4/PEEK (APC2) unidirectional laminates. The MMB delamination test introduced in this paper is rather simple and is believed to offer several advantages over most current mixed-mode test procedures.

INTRODUCTION

Failures in composite structures often develop as delaminations between plies. Typically, such delaminations initiate and propagate under the combined influence of normal and shear stresses. Therefore, tests of delamination resistance should account for the effects of combined stresses. The present study addresses delamination testing with combined tensile normal stress (mode I) and sliding shear stress (mode II). Various approaches have been used to develop test specimens with such combined normal and shear stresses on the delamination plane. Unfortunately, however, several different types of specimens are often needed to generate delamination toughness data over a desired range of mixed-mode combinations. For example, figure 1 shows interlaminar fracture toughness curves measured using three different specimen types [1]. The pure mode I values for delamination fracture toughness G_{Ic} were obtained using a split unidirectional laminate loaded as a double cantilever beam (DCB). The pure mode II values G_{IIc} were found using the same type of specimen, but subjected to three point bending; this type of test is called an end notch flexure (ENF) test [2]. However, the mode I and mode II components of mixed-mode fracture toughness (G_{Ic}^m and G_{IIc}^m respectively) were generated using cracked lap shear (CLS) and edge delamination tension (EDT) specimens [3]. The use of different test configurations can involve different test variables and analysis procedures that can influence test results in ways that are difficult to predict. The purpose of this paper is to introduce a new test apparatus that can be used to measure delamination toughness over a wide range of mode I/II ratios as well as pure mode I and mode II.

First, the current methods for mixed-mode delamination testing will be briefly reviewed. Next, the proposed mixed-mode bending (MMB) test is described. Then the total strain energy release rate G and its mode I (G_I) and mode II (G_{II}) components will be evaluated for the MMB

test specimen using a finite element analysis. In addition, closed form equations for G_I and G_{II} will be developed using simple beam theory with modifications to improve their accuracy. Finally, the MKB test method is demonstrated by testing graphite/PEEK (APC2) specimens over a wide range of G_I/G_{II} ratios. Delamination toughness data are presented in terms of the mode I and mode II components of delamination fracture toughness.

NOMENCLATURE

a	delamination length, m
b	specimen width, m
c	position of applied load on lever, m
E_{11}	lamina longitudinal modulus, GPa
E_{22}	lamina transverse modulus, GPa
G	total mixed-mode strain energy release rate, J/m^2
G_c	total mixed-mode delamination fracture toughness, J/m^2
G_{12}	lamina longitudinal shear modulus, GPa
G_{13}	lamina transverse shear modulus, GPa
G_I	mode I strain energy release rate, J/m^2
G_{II}	mode II strain energy release rate, J/m^2
G_{Ic}	delamination fracture toughness for mode I loading, J/m^2
G_{IIc}	delamination fracture toughness for mode II loading, J/m^2
G_{Ic}^m	mode I component of G_c for mixed-mode loading, J/m^2

G_{IIc}^m	mode II component of G_c for mixed-mode loading, J/m^2
h	specimen half-thickness, m
k	stiffness of elastic foundation, N/m^2
L	specimen half-span, m
P	applied load, N
P_I	mode I load, N
P_{II}	mode II bending load, N
δ	load-point displacement, m
λ	elastic foundation parameter, $1/m$
ν_{12}	lamina Poisson's ratio

CURRENT MIXED-MODE DELAMINATION TESTS

This section briefly reviews current approaches for mixed-mode delamination testing. This review provides background for the new approach presented in the next section. Combined mode I and mode II delamination fracture toughness tests usually employ a specimen containing an artificially introduced delamination. The specimen is loaded until the delamination grows. Measured load and delamination length can then be substituted into strain energy release rate equations to calculate the delamination toughness.

A sketch of the cracked lap shear (CLS) specimen is shown in figure 2(a). Uniaxial loading is applied to one arm of a split unidirectional laminate. The load transfer to the other arm causes interlaminar normal stresses (mode I) and interlaminar shear stresses (mode II). Although the CLS specimen can be tested in conventional tension test machines, it has several serious limitations. First, the mode I/II ratios cannot be calculated by simple closed form stress analyses, and therefore, a numerical analysis is required. Further, because large rotations can result from the load eccentricity at the delamination front, a geometrically nonlinear numerical

analysis may be required to evaluate G_{II} and G_{II} [4]. Also, different ply layups are required to create different mode I/II combinations, and only a rather narrow range of ratios is attainable.

The edge delamination tension (EDT) specimen, shown in figure 2(b), was developed by O'Brien [3]. A specimen with a layup such as (+35/0/90) is loaded in tension and the mismatch in the Poisson's ratios of the plies causes high edge stresses at the 0/90 ply interfaces. The load-induced mode I and mode II stresses at these interfaces can initiate edge delaminations. Unfortunately, however, hygrothermal interlaminar stresses also exist at this interface and can seriously reduce the measured delamination toughness [5]. Also, numerical analyses are required to calculate the interlaminar G_I and G_{II} components in the EDT test.

In the Arcan test configuration [6], figure 2(c), a split unidirectional laminate is bonded between two metal fixtures that can be loaded to produce various mixed-mode conditions at the delamination front. But, as with the CLS and EDT tests, the mode I/II ratio must be determined by a numerical analysis. Also, bond failures can limit the Arcan test use, especially for tough laminates.

The asymmetric DCB test, proposed by Bradley and Cohen [7], avoids most of the problems found with the first three methods. As shown in figure 2(d), this approach involves loading the arms of a unidirectional DCB specimen with two different loads. The loads can be selected to produce the full range of mode I/II ratios. Equal and opposite loads produce a pure mode I delamination, and equal loads produce a pure mode II delamination. Unfortunately, the asymmetric DCB approach requires a complex loading system to simultaneously control the two applied loads.

The mixed-mode flexure test, proposed by Russell and Street [8], is shown in figure 2(e). This test specimen is similar to the CLS specimen but is loaded in three point bending. Unfortunately, different arm thicknesses are required to produce different mode I/II ratios. This

requires that specimens be fabricated with the delamination starter at different ply interfaces. Also different arm thicknesses can influence the stress distribution ahead of the delamination [9] and, therefore, may influence toughness measurements.

The variable mixed-mode test in figure 2(f) was proposed by Hashemi, Kinloch, and Williams [10]. A pure mode II condition is created when the delamination tip is centered under the mid-span tension load. The mode I/II ratio increases as the delamination extends toward the left load point. A pure mode I condition exists when the delamination is under the left load point. As a result, the full range of mode I/II ratios can be produced. However, the ratio changes as the delamination grows. This could complicate the data analysis, especially for large increments of unstable growth. Also, when the delamination tip is near either load point, simple closed form equations for G_I and G_{II} will not account for the complex effects of load concentrations or loading fixture stiffness.

MIXED-MODE BENDING TEST

The mixed-mode bending (MMB) test simply combines the mode I DCB and the mode II ENF tests. This is achieved by adding an opening-mode load to a midspan loaded ENF specimen, as shown in figure 3(a). This additional load separates the arms of the split unidirectional laminate as in a DCB test. The relative magnitudes of the two applied loads determines the mixed-mode ratio at the delamination front. By applying these two loads through a lever and hinge apparatus as shown in figure 3(b), the test can be conducted by applying a single load. The loading position c determines the relative magnitude of the two resulting loads on the specimen and, therefore, determines the mixed-mode delamination ratio. Pure mode II loading occurs when the applied load is directly above the beam mid-span ($c = 0$). Pure mode I loading can be achieved by removing the beam and pulling up on the hinge.

A photograph of the MMB test apparatus is shown in figure 4. The loading lever is an aluminum I-beam weighing only 6 N, which was assumed to be a negligible weight. The lever is several orders of magnitude stiffer than the specimen and therefore, was assumed to be rigid. The lever load, the mid-span load, and the left support reaction are applied through bearing-mounted rollers to reduced frictional forces. The right end of the specimen is loaded through high-quality, extruded aluminum hinges bonded to the specimen arms. The specimen in this photograph is a 24-ply graphite/PEEK unidirectional laminate, 25 mm wide and 102 mm long. The apparatus is mounted on a thick steel base.

STRESS ANALYSIS

This section presents the stress analysis of the MMB test specimen and focuses on the calculation of strain energy release rates. The G_I/G_{II} ratio is needed to resolve the measured mixed-mode delamination fracture toughness G_c into its mode I and mode II components, G_{Ic}^m and G_{IIc}^m , respectively. First, a finite element analysis was used to provide a basic understanding of the strain energy release rate during MMB testing. Next, a more convenient beam theory analysis is presented and its results are compared with those from the finite element analysis. Finally, the simple beam theory analysis was modified to improve its accuracy.

Finite Element Analysis

The MMB specimen was modeled and loaded as shown in figure 5. Eight-noded quadrilateral elements were used with the MSC NASTRAN finite element code [11]. To account for the effect of an uneven fiber distribution through the specimen thickness, an effective modulus was calculated from a 3-point bend test [12]. Measured mid-span displacements and

loads were used with beam theory to calculate the longitudinal modulus E_{11} for the laminate. An effective E_{11} of 116 GPa was determined by this approach, compared to the uniaxial tension value of 129 GPa from [13]. A transverse modulus E_{22} of 10.1 GPa, a Poisson's ratio γ_{12} of 0.329, and shear modulus G_{12} of 5.5 MPa were used [13].

The finite element modeling was evaluated by comparing the computed load-displacement results with measured results. The solid line in figure 6 represents the computed finite element results and the symbols show measurements taken during loading and unloading of the MMB apparatus. The load-point displacement was determined from the crosshead position. The solid curve agrees with the test data very well in the lower load range and slightly over estimates the displacements in the upper range. The discrepancy may be caused by geometric nonlinearity, which was not accounted for by the finite element analysis. However, the correlation in this figure does suggest that the finite element model is sufficiently accurate to analyze the MMB specimen. Crack tip forces and displacements were used in the virtual crack closure technique [14] to calculate G_I and G_{II} for the MMB specimen.

As previously mentioned, the load position c determines the ratio of the mode I and mode II. To establish a relationship between c and the G_I/G_{II} ratio, the finite element analysis was repeated for several values of c . This relationship is shown in figure 7 where the symbols are the computed values and the solid line is a best-fit curve. The test data shown previously in figure 1 suggest that a mixed-mode toughness curve could be established reasonably well using five test cases: three mixed-mode and the two pure mode toughness tests. In the present study, mixed-mode ratios of 4/1, 1/1, and 1/4 were selected. As shown in figure 7, the three corresponding c values are 95 mm, 41 mm, and 27 mm, respectively. Although the present study was limited to three mixed-mode ratios, the MMB apparatus can be used to measure any G_I/G_{II} ratio from zero to approximately five. Notice that G_I/G_{II} is zero for c less than about 18 mm. Below this value,

the mode I loading is not large enough to overcome the crack-face normal stresses produced by the mode II loading. Hence, the delamination does not open, and G_I must be zero within this range, despite the nonzero c values. As previously mentioned, the mode II tests were conducted with c equal to zero.

Finite element analyses of the MMB specimen were conducted to determine the variation of the strain energy release rate during delamination. A half-span length of 50 mm was used and analyses were conducted for delamination lengths from about 20 mm to 45 mm. Figure 8 shows computed values of total strain energy release rate G for the pure mode I and mode II cases, plotted over a range of delamination lengths. The two curves in this figure represent limits for the mixed-mode cases. For convenience, G values are normalized by the square of the load-point displacement. If the curves are interpreted as G variations during delamination growth under constant displacement δ , then they can be compared with toughness G_c to predict if delamination growth is unstable (G continues to equal or exceed G_c as the delamination grows) or is stable (G falls below G_c) requiring additional loading for subsequent growth. The negative slope of the mode I curve shows that delamination growth in a DCB test should be stable. In contrast, the peak of the mode II curve at 35 mm suggests delamination growth would be unstable for delamination lengths less than this value but stable for longer lengths.

The C/δ^2 curves for the three mixed-mode loading cases are shown in figure 9. The case where mode I is dominant ($G_I/G_{II} = 4/1$) has a curve with a negative slope, which indicates stable delamination growth as in the pure mode I case shown in figure 8. The 1/1 and the 1/4 curve both indicate a region of unstable growth below delamination lengths of 25 mm and 30 mm, respectively. As expected, a higher mode II component in the mixed-mode test results in a larger region of instability. Figure 10 shows the G_I and G_{II} component curves for the three mixed-mode cases. These curves have the same trends as the total G curves in figure 9.

The G_I and G_{II} values shown in figure 10 were used to calculate the G_I/G_{II} ratios which are plotted versus delamination length in figure 11. Preferably, this ratio should be constant throughout the test range of delamination lengths. The horizontal lines in figure 11 represent the 4/1, 1/1, and 1/4 mixed-mode ratios and pass through the computed values for the 25 mm delamination length. (Recall that a 25 mm delamination length was used in figure 7 to establish the load position c for each of the three mixed-mode cases). Within the useful test range (delamination lengths from 25 mm to 45 mm), the G_I/G_{II} ratios deviated from the nominal values by only about 5 percent. This small deviation shows that the G_I/G_{II} ratio can be assumed to be constant during delamination growth for the MMB test.

Beam Theory Analysis

Although the finite element analysis provided an accurate strain energy release rate analysis of the MMB specimen, a closed form analysis offers many advantages in setting up MMB tests and evaluating test results. A closed form analysis also shows the functional relationships among the test parameters, which improves the basic understanding of the MMB test. This section presents strain energy release rate equations based on beam theory. The MMB loading was represented by a superposition of simple mode I and mode II loadings, equivalent to those used with DCB and ENF tests, respectively. Thus, strain energy release rate equations from the literature on DCB and ENF tests could be combined to obtain the desired equations for the MMB test.

Figure 12(a) shows the MMB loading expressed in terms of the applied load P , the loading lever length c , and the specimen half-span L . As shown in figure 12(b), the mode I component of this loading is

$$P_I = \left(\frac{3c-L}{4L}\right)P$$

Simple beam theory analysis of the DCB specimen leads to

$$G_I = \frac{12a^2P_I^2}{b^2h^3E_{11}} \quad (1)$$

where b is specimen width and h is half-thickness. Substituting for leads to the following equation for G_I of the MMB test.

$$G_I = \frac{3a^2P^2}{4b^2h^3L^2E_{11}} (3c-L)^2 \quad (2)$$

Figure 12(c) shows the mode II portion of the MMB loading. Note that the right end loading has been divided equally between the two equal-stiffness arms of the specimen. This is equivalent to the conventional loading of the ENF test. For the ENF test, the mode II bending load is

$$P_{II} = \left(\frac{c+L}{L}\right)P$$

as shown in figure 12(c). The following equation for G_{II} of the ENF test was presented in [2].

$$G_{II} = \frac{9a^2P_{II}^2}{16b^2h^3E_{11}} \quad (3)$$

Substituting for P_{II} , the corresponding equation for G_{II} of the MMB test is

$$G_{II} = \frac{9a^2P^2}{16b^2h^3L^2E_{11}} (c+L)^2 \quad (4)$$

By dividing equation (2) by equation (4), the G_I/G_{II} ratio for the MMB test can be expressed as

$$G_I/G_{II} = \frac{4}{3} \left[\frac{(3c-L)}{(c+L)} \right]^2 \quad c \geq \frac{L}{3} \quad (5)$$

Notice that G_I/G_{II} is only a function of load position c and half-span length L . The G_I/G_{II} ratio is zero for $c = L/3$ ($c = 17$ mm for the present study), and equation (5) is invalid for smaller c values because this model does not account for contact between the two arms of the specimen. The total strain energy release rate for the MMB test is obtained by adding equations (2) and (4).

$$G = \frac{3a^2P^2}{16b^2h^3L^2E_{11}} \left[4(3c-L)^2 + 3(c+L)^2 \right] \quad (6)$$

Equation (6) is compared with the finite element results in figure 13. These results for a 25 mm delamination with G_I/G_{II} equal to unity show that equation (6) underestimates G by about 15 percent. To analyze this discrepancy, G_I and G_{II} were calculated using equations (2) and (4) and are compared with the corresponding finite element results in figure 14. The G_I values are 18 percent low while the G_{II} values are only 6 percent low. This indicates that most of the error in equation (6) can be attributed to the G_I component and, therefore, to the beam theory equation for the DGB test.

Kanninen [15] introduced an improved beam theory equation for the DCB test. He recognized that simple beam theory did not properly model the interaction between the two arms of the DGB specimen. The two arms are not fixed against rotation at the delamination tip as assumed in simple beam theory. Instead, they rotate slightly due to the elastic support that they provide one another. To account for this, Kanninen assumed that each arm was a beam supported by an elastic foundation. His analysis of an isotropic DCB specimen was extended to an orthotropic DCB specimen by replacing E with E_{11} and E_{22} (Personal communication with K. N. Shivakumar, Analytical Services & Materials, Inc., 28 Research Drive, Hampton, VA. 23666).

$$G_I = \frac{12P_I^2}{b^2 h^3 E_{11}} \left[a^2 + \frac{2a}{\lambda} + \frac{1}{\lambda^2} \right] \quad (7)$$

where $\lambda = (3k/bh^3 E_{11})^{1/4}$

and $k = 2bE_{22}/h$

The beam theory equations for strain energy release rate can be further improved by accounting for the shear deformation energy associated with bending. Adding the shear deformation component of strain energy release rate [16] to equation (7) leads to the following modified beam theory equation for G_I in the MMB test.

$$G_I = \frac{3P^2(3c-L)^2}{4b^2 h^3 L^2 E_{11}} \left[a^2 + \frac{2a}{\lambda} + \frac{1}{\lambda^2} + \frac{h^2 E_{11}}{10G_{13}} \right] \quad (8)$$

Similarly, adding the shear deformation term from [17] to equation (4) results in a modified beam theory equation for G_{II} in the MMB test.

$$G_{II} = \frac{9P^2(c+L)^2}{16b^2 h^3 L^2 E_{11}} \left[a^2 + \frac{0.2h^2 E_{11}}{G_{13}} \right] \quad (9)$$

Assuming the unidirectional composite specimens used in the present study are transversely isotropic, the shear modulus G_{13} in these two equations can be replaced by G_{12} .

The total G values for the MMB test were recalculated using the modified beam theory equations (8) and (9). Figure 15 compares the G calculations for the three beam theory equations with the finite element results. For the earlier case of G_I/G_{II} equal to unity, G calculated with the elastic foundation correction (dash-dot curve) agreed with the finite element values (solid curve) with an error of about 8 percent compared to the 14 percent error for the simple beam theory (dashed curve). The additional modification for shear deformation led to the dash-double dot curve, which is within about 6 percent of the finite element results. The corresponding errors for the 4/1 and 1/4 cases were also only about 6 percent.

Next, equations (8) and (9) were used to recalculate the G_I/G_{II} ratios for the three mixed-mode test cases. Recall that the values of c for the three G_I/G_{II} ratios of 4/1, 1/1, and 1/4 were selected earlier using finite element results for a 25 mm delamination (see figure 7). The recalculated G_I/G_{II} ratios are shown as the solid curves in figure 16 and are compared with the discrete finite element values, shown by symbols. These curves agree very well with the finite element values. Within the 25 mm to 45 mm range of delamination lengths, the modified beam theory ratios vary by about 3, 5, and 8 percent from the finite element results for the 4/1, 1/1 and 1/4 cases, respectively.

Compared to the finite element analysis, the modified beam theory equation (8) and (9) appear to provide acceptably accurate values of G_I and G_{II} for the MMB test. Before testing, equations (8) and (9) can be used to select the loading positions that produce desired G_I/G_{II} test ratios. After testing, measured values of delamination length and the corresponding MMB specimen loads can be substituted into these equations to calculate the mode I and mode II delamination fracture toughness components, G_{Ic}^m and G_{IIc}^m .

TEST RESULTS

As previously mentioned, tests were conducted with 24-ply unidirectional AS4/PEEK (APC2) specimens. These specimens were 25 mm wide and contained a Kapton film delamination starter at one end of the specimen. The Kapton film was 25 mm wide, 35 mm long, 13 μ m thick and located at the specimen mid-plane. To produce a initial delamination, each specimen was precracked to about 30 mm using the 4/1 mixed-mode ratio. G_I/G_{II} mixed-mode ratios of 4/1, 1/1, and 1/4 were produced by selecting the load positions from figure 7. Pure mode II tests were conducted by applying the load at the specimen mid-span ($c = 0$). For the pure

mode I case, the loading lever was removed and an upward load was applied directly through the upper hinge on the specimen. Each specimen was loaded under displacement control at a rate of 0.5 mm/min until the delamination grew. The maximum load was recorded and the delamination length was measured visually at the specimen edges. The edges had been coated with white water soluble typewriter correction fluid to make the delamination easier to see.

The delamination growth was usually stable, and delamination growth increments were about 5 mm. The tests were stopped when the delamination reached 45 mm length and specimens were split apart to examine the markings usually produced by the loading-unloading sequence. These markings provided accurate measurements of delamination length and were used to verify the measurements taken during testing. The recorded values for load and delamination length were used in equations (8) and (9) to calculate G_{Ic}^m and G_{IIc}^m , respectively.

Test results are presented in figure 17 with G_{Ic}^m plotted against G_{IIc}^m . Each symbol represents a toughness measurement corresponding to growth from the precrack. The solid curve fitted through the data can be viewed as a delamination failure criterion for mixed-mode loading. The curve is nearly horizontal in the region where $G_I/G_{II} > 1$ indicating that the toughness is nearly independent of G_{II} and, therefore, that delamination growth was controlled by mode I loading. In the region where $G_I/G_{II} < 1$, the curve is sloped indicating that both mode I and mode II loading influence the delamination toughness. The test results are tabulated in Table 1.

Table 1 also shows the fracture toughness data obtained during specimen precracking. Recall that all specimens were precracked by extending the delamination from the starter insert using a G_I/G_{II} ratio of 4/1. The average toughness for delamination growth from the insert was only about 2 percent lower than growth from the precrack with the 4/1 loading. This suggests that the precracking was unnecessary. However, a comprehensive study of precracking was beyond the scope of this initial demonstration of the MMB test.

CONCLUDING REMARKS

A mixed-mode bending (MMB) delamination test procedure has been presented for a split unidirectional laminate. The mixed-mode loading was created by combining the mode I loading for the double cantilever beam (DCB) test with that for the mode II end notch flexure (ENF) test. This combined loading was produced using a loading lever, and the ratio of mode I to mode II was varied by changing the load position on the lever. Both finite element analysis and beam theory analyses were conducted to determine the mode I and mode II components of strain energy release rate, G_I and G_{II} , respectively. The MMB test procedure was demonstrated by measuring the mixed-mode delamination fracture toughness of AS4/PEEK (APC2) unidirectional laminates.

Finite element analyses were conducted to determine the loading lever lengths necessary to produce the desired mixed-mode ratios of 4/1, 1/1, and 1/4. The finite element analysis showed that these ratios varied by less than 5 percent over a 20 mm test range of delamination lengths. Therefore, the G_I/G_{II} ratio can be assumed to be independent of delamination length. Beam theory equations from the literature for double cantilever beam (DCB) and end notch flexure (ENF) tests were used with a superposition procedure to develop equations for the G_I and G_{II} for the MMB test. These equations were then modified using elastic foundation and shear deformation analyses. The resulting modified equations for G_I and G_{II} were within about six percent of the finite element results. Measured delamination lengths and loads from the MMB tests were substituted into these equations to determine the mode I and mode II components of delamination toughness during mixed-mode delamination. Pure mode I and mode II tests were also conducted by simplifying the MMB test to produce DCB and ENF loadings, respectively. This approach provided delamination fracture toughness data over a wide range of G_I/G_{II} ratios

using identical test specimens and procedures.

The MMB test is a rather simple and direct combination of DCB and ENF tests and seems to offer several advantages over most current mixed-mode delamination tests. Many of the data reduction procedures that have been developed for the DCB and ENF tests should be applicable to the MMB test because of its similarities with these pure-mode tests. Also, DCB and ENF studies of test parameters such as insert thickness and precracking may be applicable to the MMB test. Therefore, it should be relatively easy to use MMB testing beyond the initial procedures of the present study.

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Table 1. - Delamination fracture toughness data for AS4/PEEK (APC2).

Test type	Specimen number	Delamination		G_{Ic}^m (kJ/m ²)	G_{IIc}^m (kJ/m ²)
		Type ^a	Length (mm)		
DCB	12	P	37.1	1.63	0.00
	28	P	34.0	1.24	0.00
	31	P	31.8	1.08	0.00
	46	P	33.4	0.88	0.00
	52	P	35.3	1.31	0.00
4/1	17	P	30.7	1.25	0.33
	35	P	32.1	0.99	0.26
	37	P	32.2	1.11	0.29
	53	P	32.5	1.50	0.39
	23	I	25.7	1.13	0.29
	25	I	25.7	0.96	0.25
	26	I	25.4	1.14	0.29
	27	I	25.4	1.15	0.30
	28	I	25.0	1.31	0.34
	31	I	25.7	1.14	0.29
	32	I	24.8	1.07	0.27
	34	I	26.8	1.21	0.31
	35	I	25.9	1.13	0.29
	36	I	24.6	1.29	0.33
	37	I	22.6	1.24	0.31
	38	I	21.4	1.30	0.33
	45	I	25.4	1.17	0.30
	46	I	25.4	1.11	0.29
	52	I	25.4	1.42	0.36
	53	I	25.4	1.29	0.33
1/1	16	P	33.7	1.18	1.27
	27	P	32.0	1.47	1.57
	34	P	31.8	1.33	1.42
	36	P	36.8	1.33	1.44
1/4	18	P	33.3	0.55	2.49
	25	P	32.9	0.44	1.98
	26	P	38.1	0.54	2.44
	32	P	30.9	0.52	2.34
	45	P	38.5	0.46	2.09
ENF	14	P	38.9	0.00	2.38
	22	P	33.3	0.00	2.88
	23	P	32.5	0.00	2.38
	38	P	33.4	0.00	2.50

a -- P - Growth from 4/1 precrack; I - Growth from delamination insert.

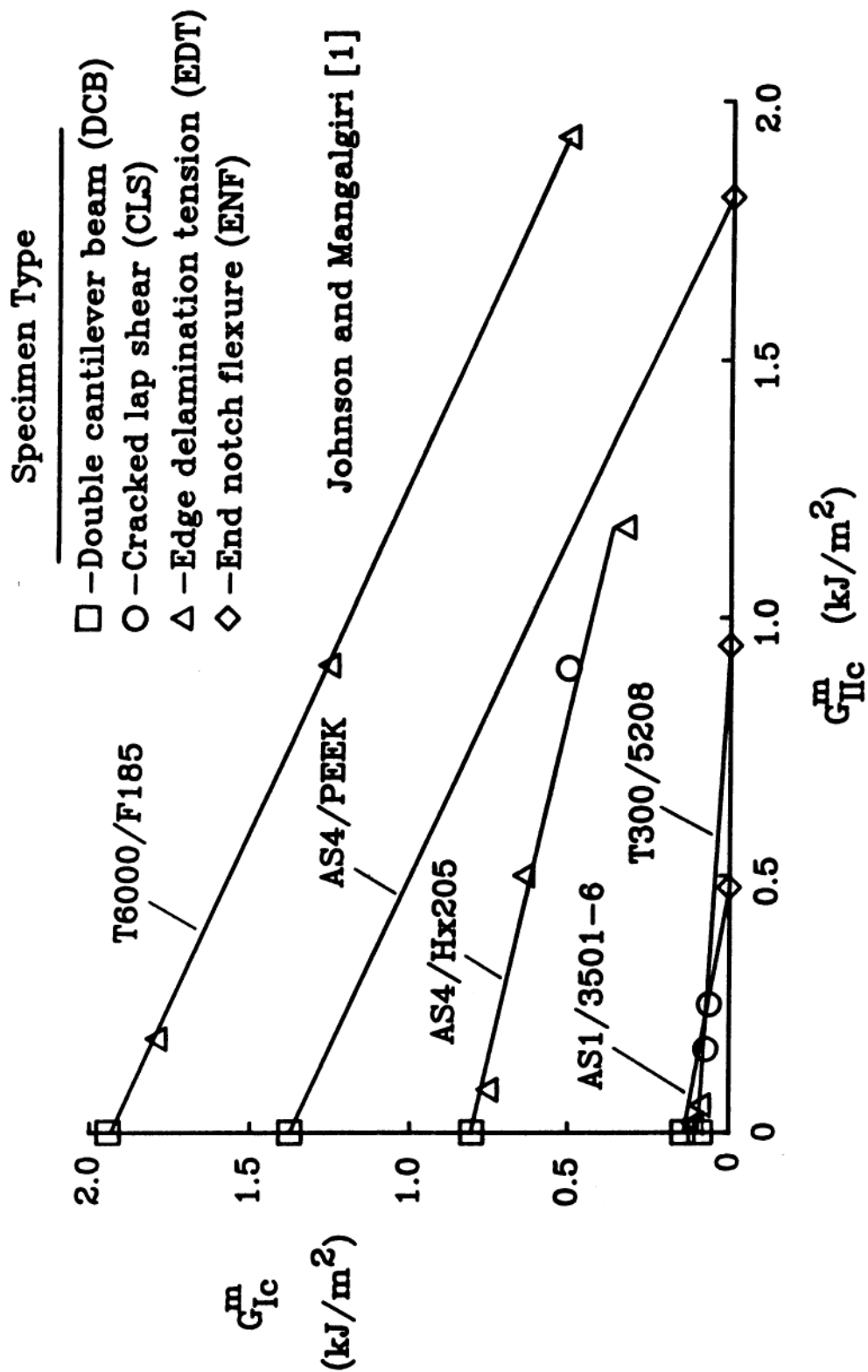


Figure 1. – Delamination toughness for mixed mode I and mode II loading.

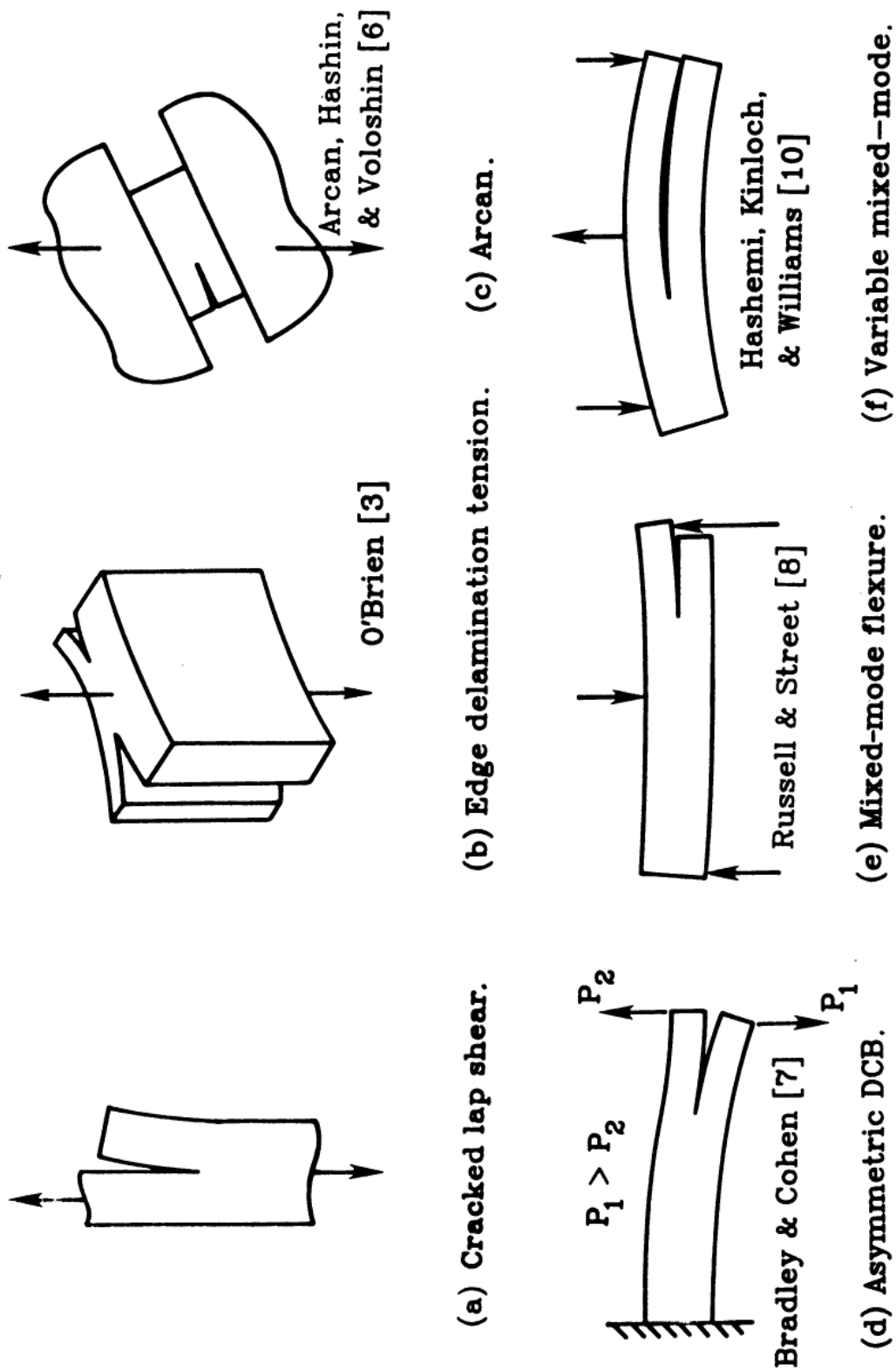
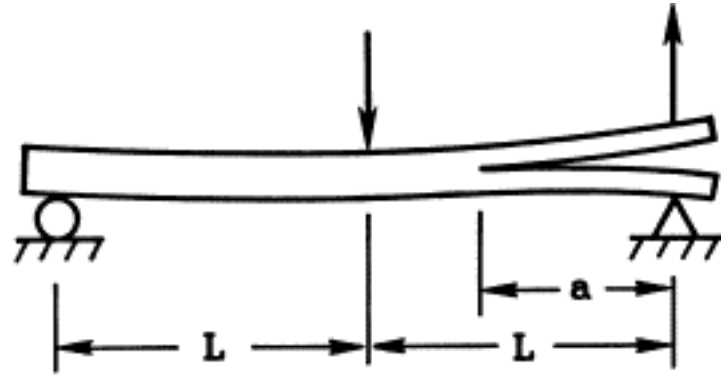
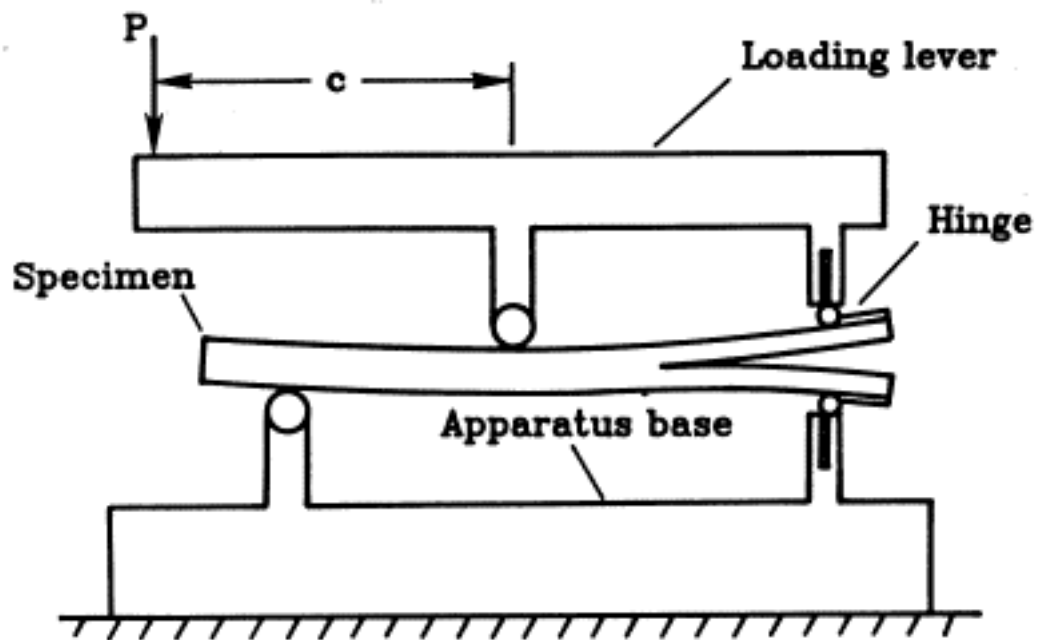


Figure 2. – Mixed mode I and II delamination test specimens.



(a) Test specimen and loading.



(b) Schematic diagram of apparatus.

Figure 3. – Mixed-mode bending specimen and test apparatus.

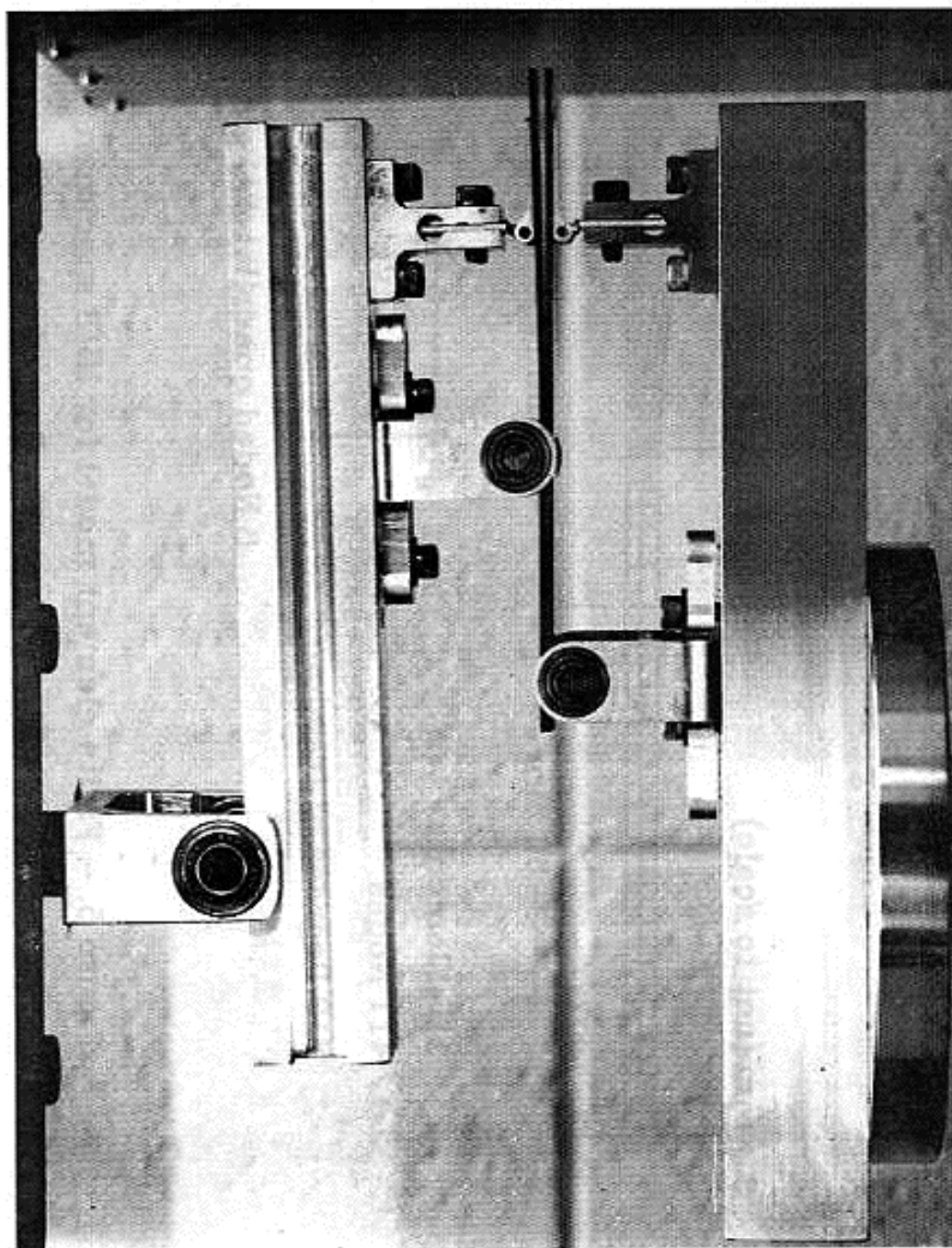
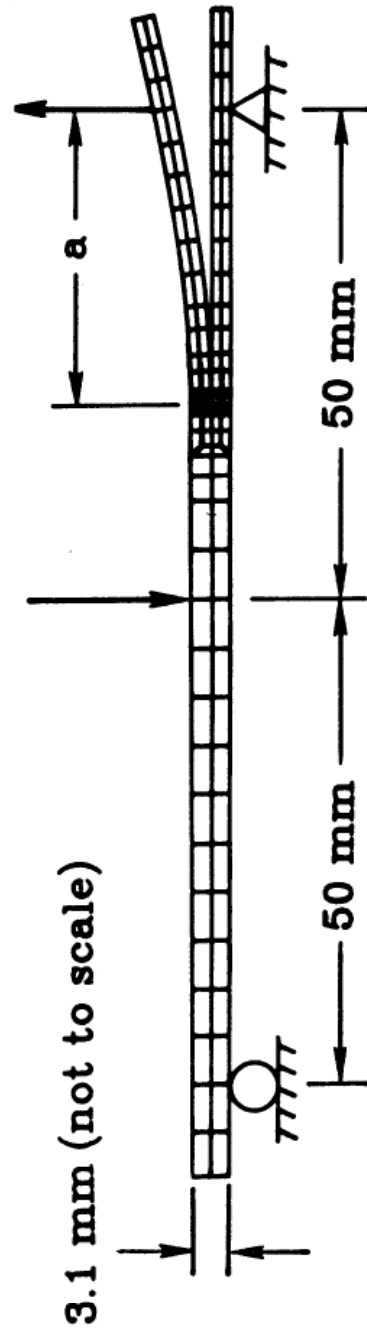


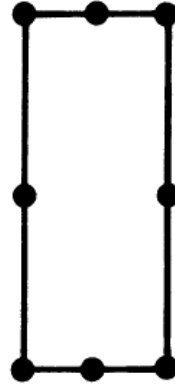
Figure 4. - Photograph of MMB test apparatus.



110 Elements

411 Nodes

819 Degrees of freedom



8 Noded quadrilateral element

Figure 5. – Finite element model for MMB specimen.

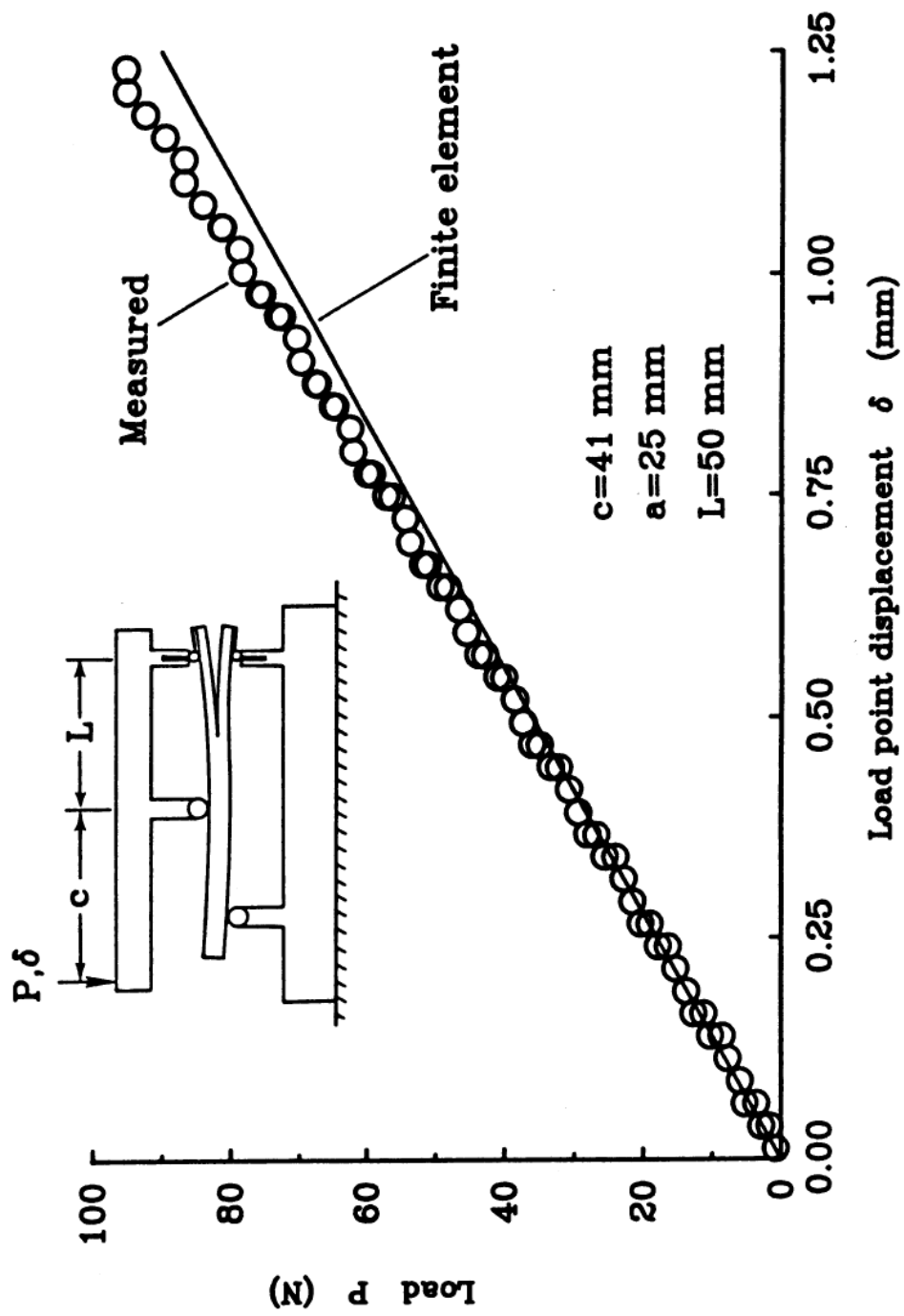


Figure 6. – Comparison of computed and measured load–displacement curves.

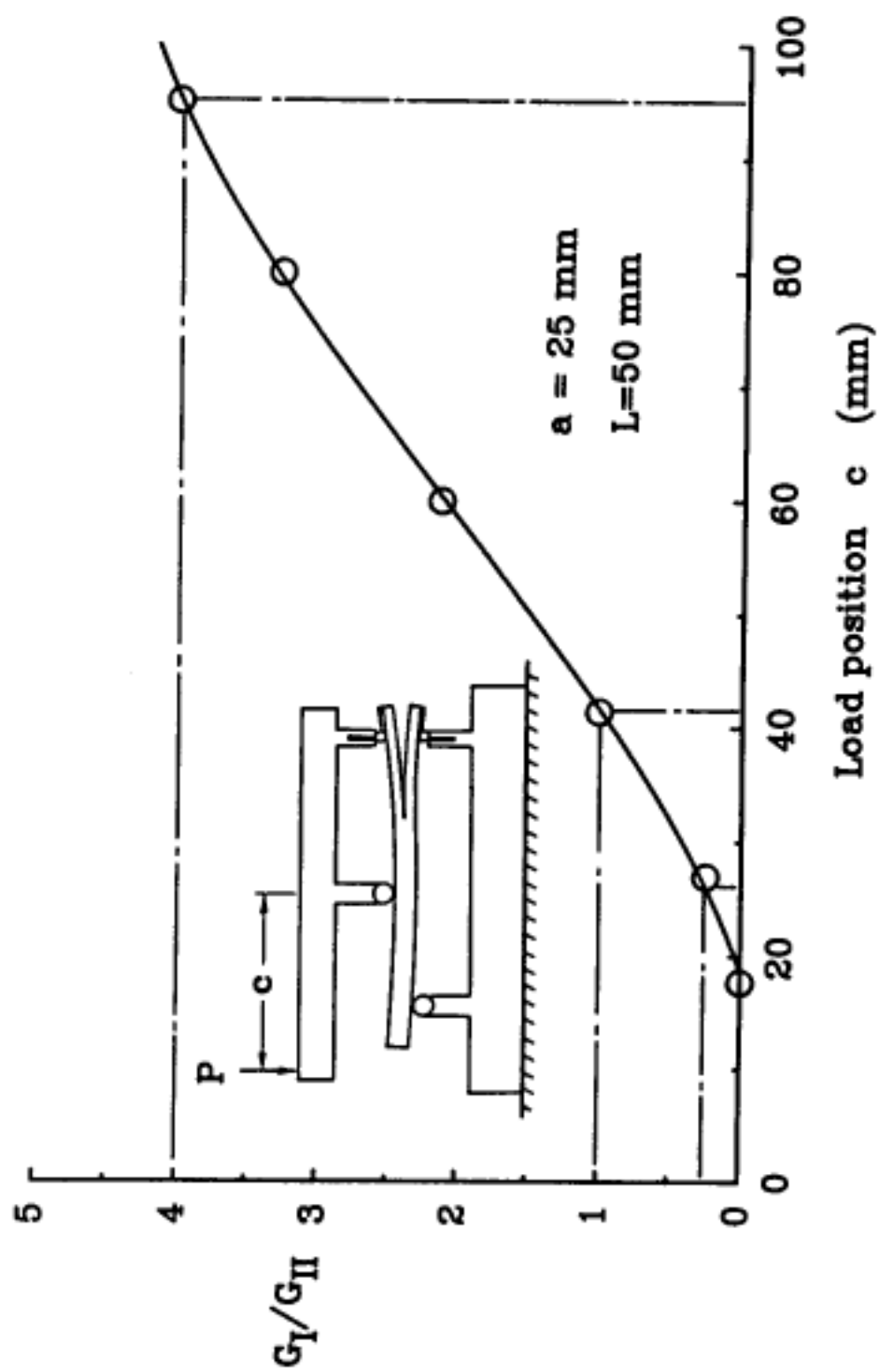


Figure 7. -- Load position for mixed-mode testing.

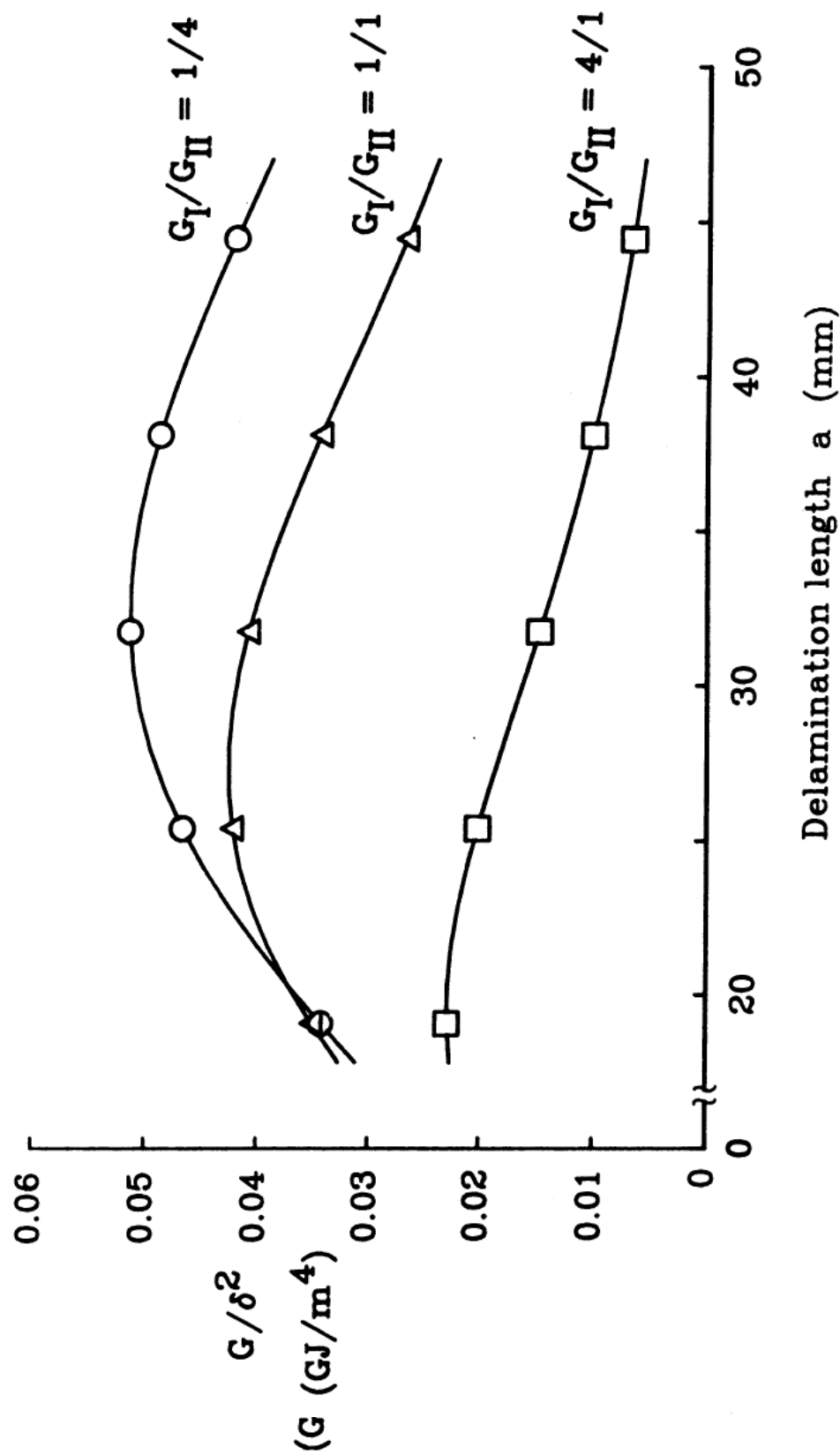


Figure 9. – Strain energy release rates for mixed-mode loading.

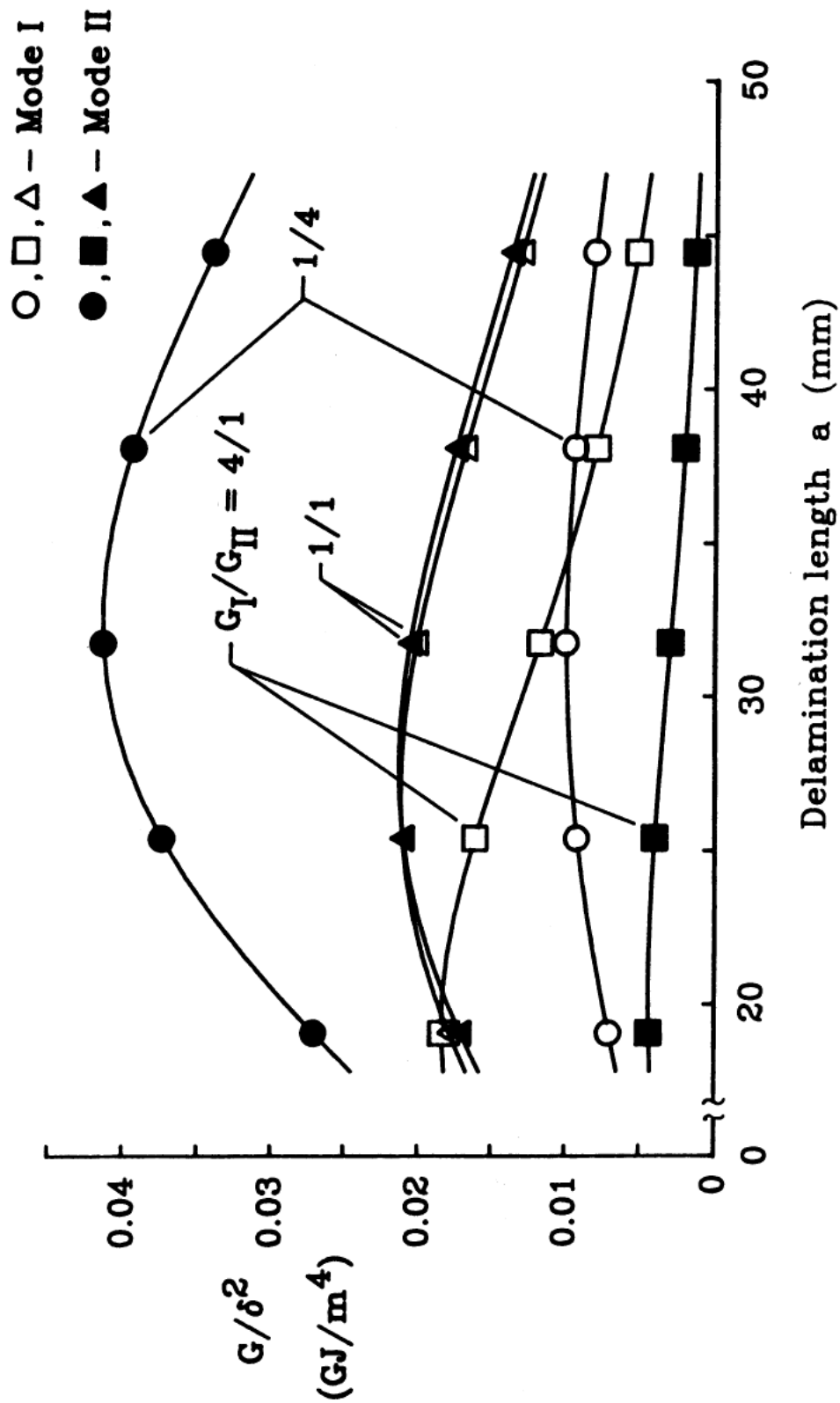


Figure 10. - Mode I and II components of strain energy release rates for mixed-mode loading.

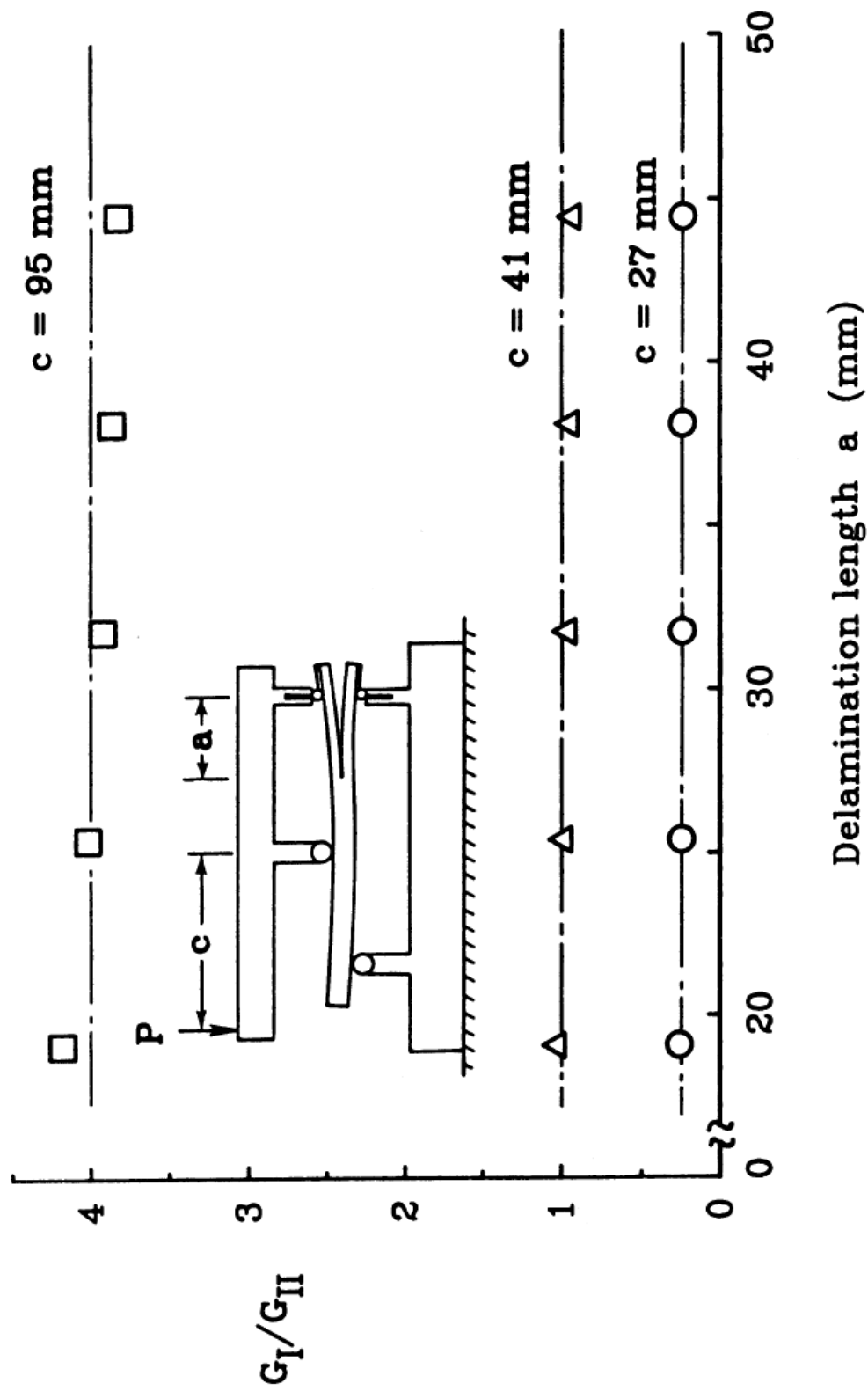


Figure 11. – G_I/G_{II} ratio for mixed-mode loading.

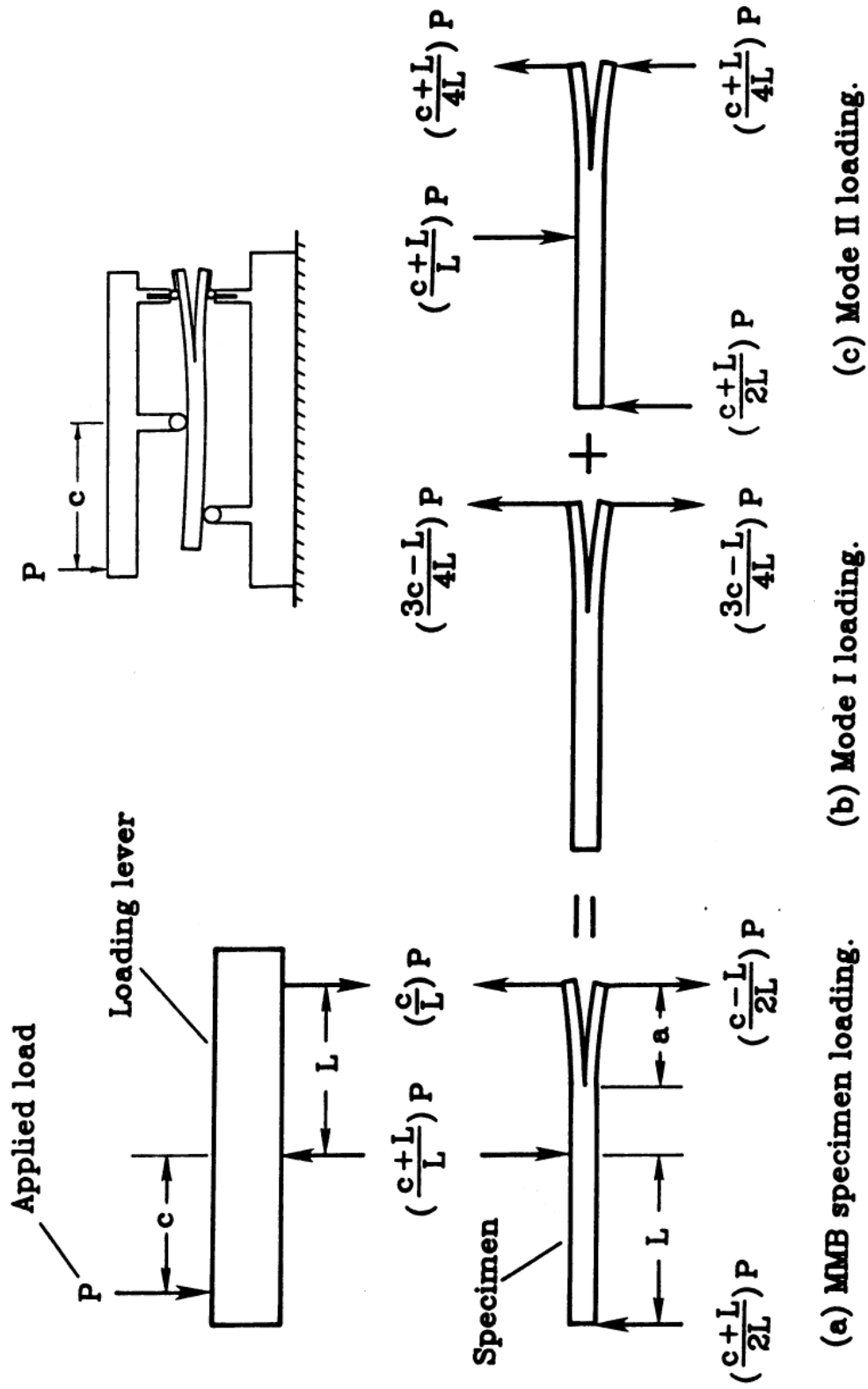


Figure 12. – Superposition analysis of loading on MMB specimen.

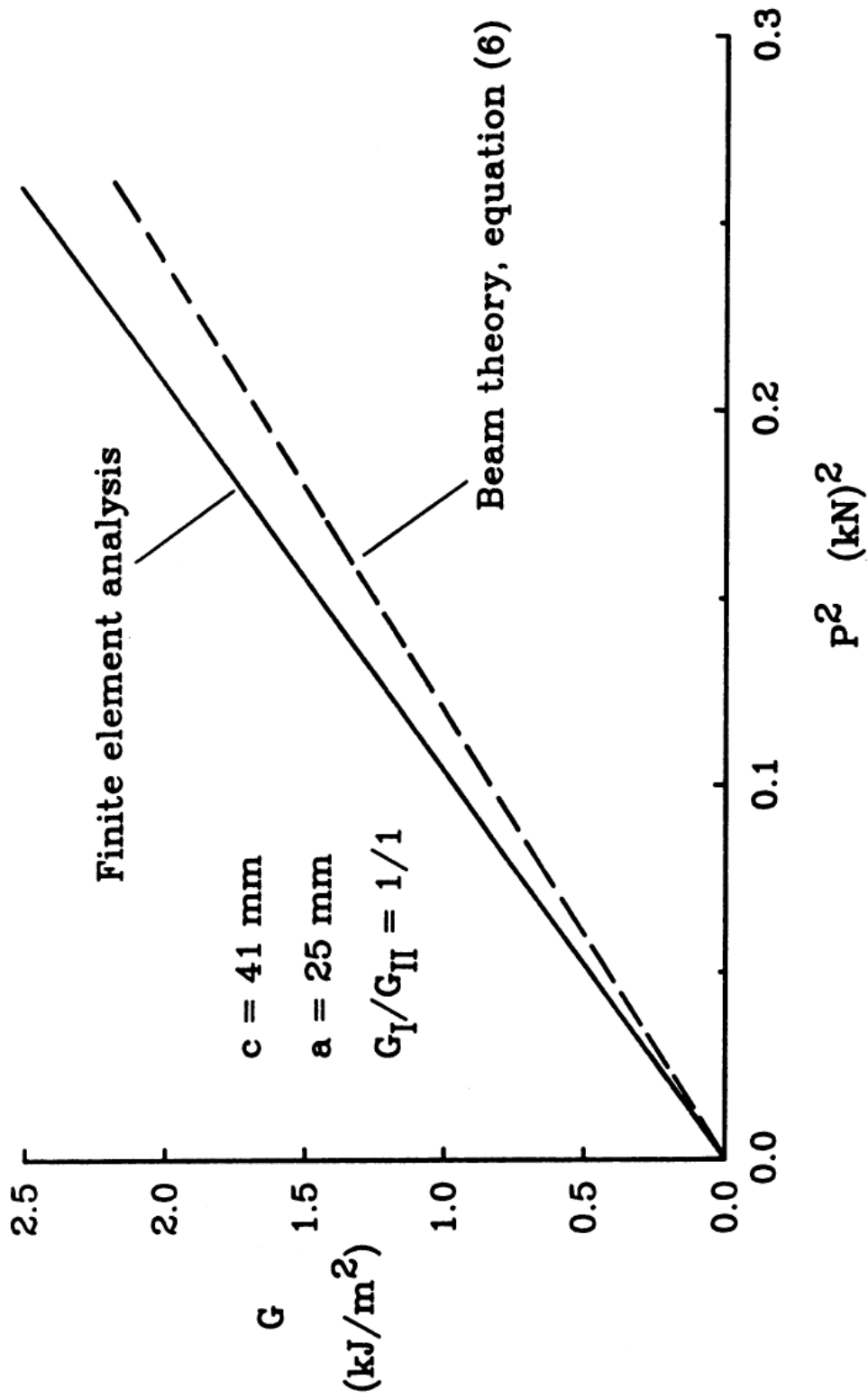


Figure 13. – Comparison of beam theory and finite element results.

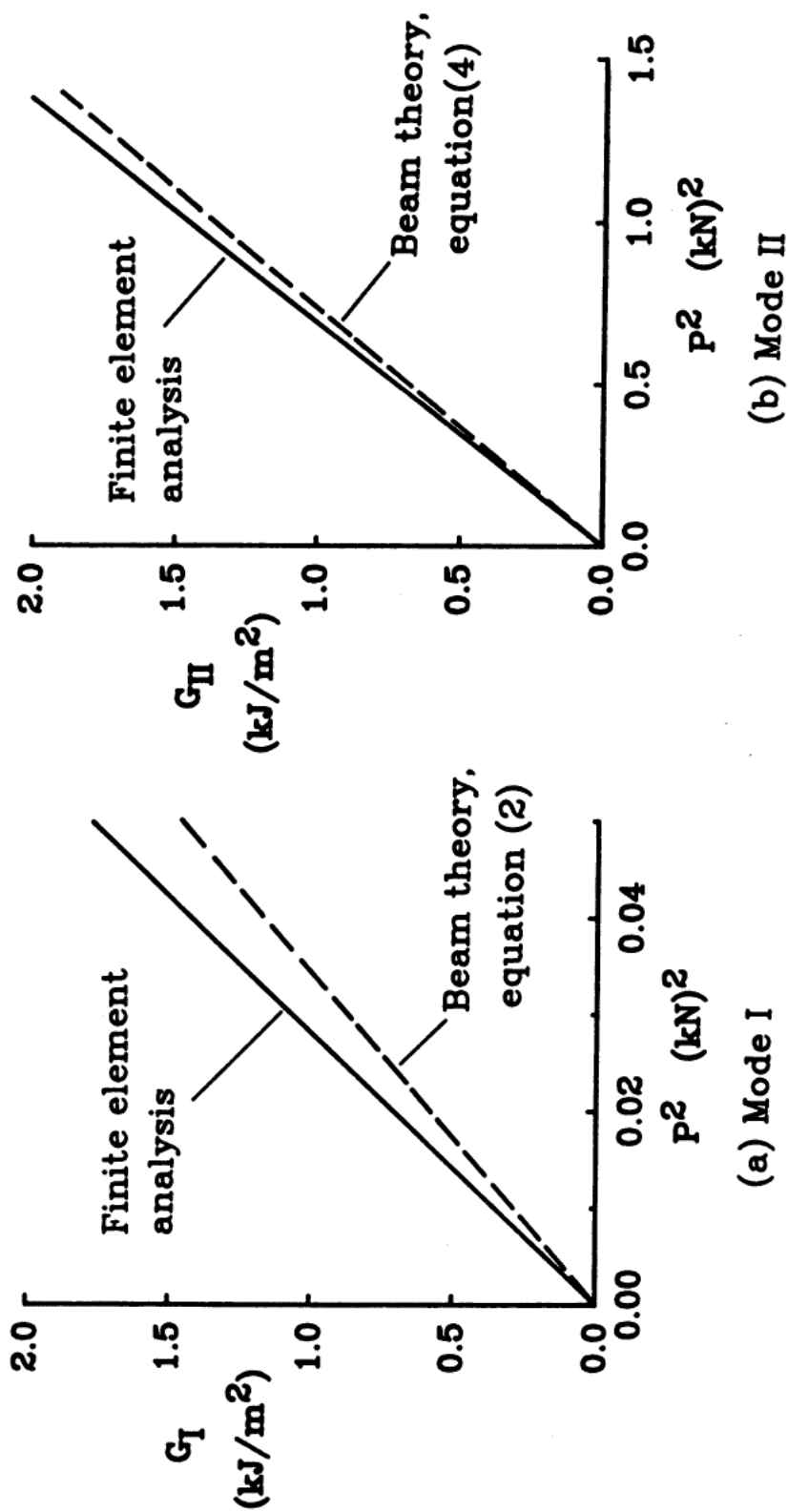


Figure 14. – G_I and G_{II} components from beam theory and finite element analysis.

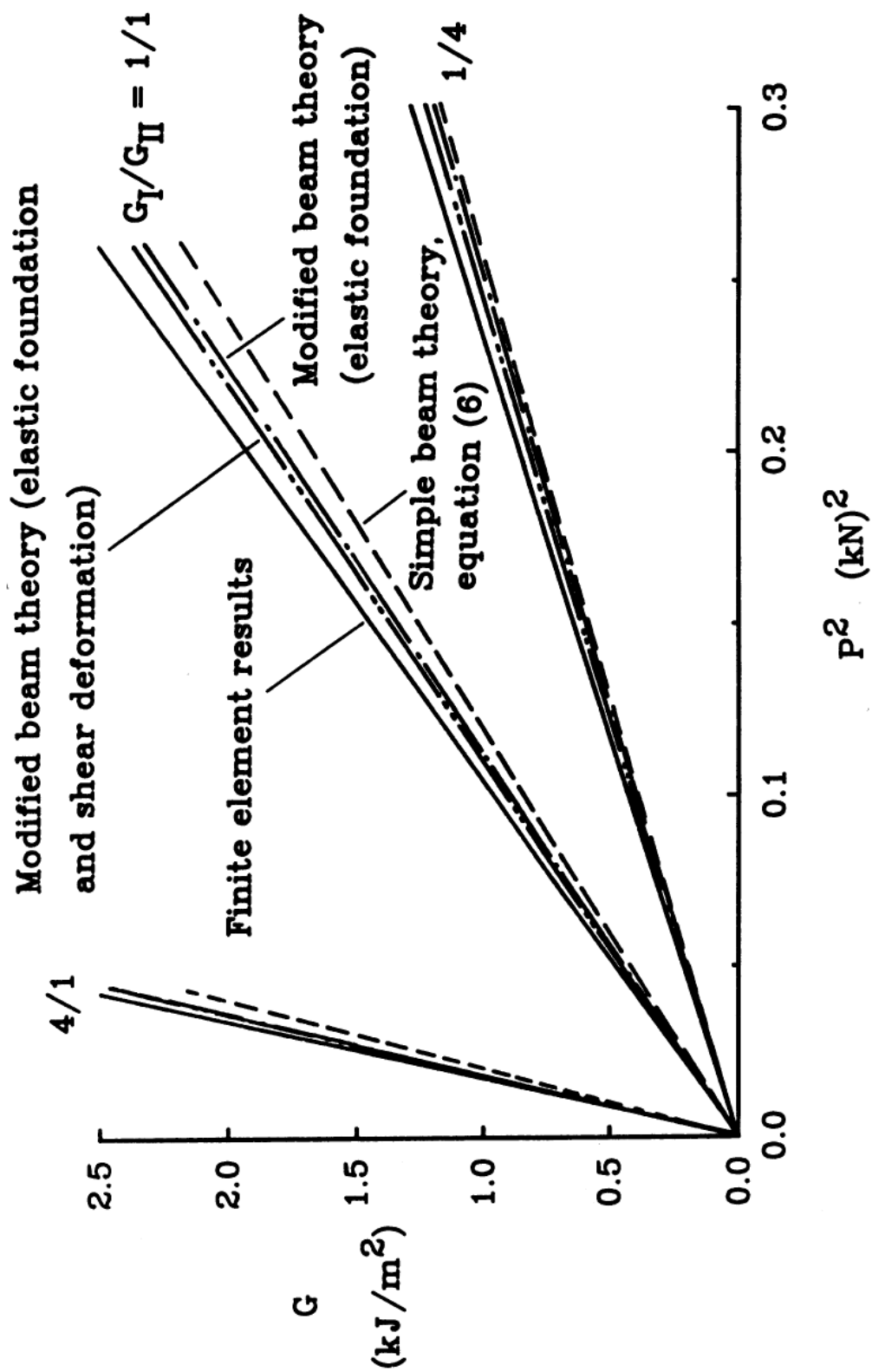


Figure 15. – Comparison of G results for mixed-mode loading cases.

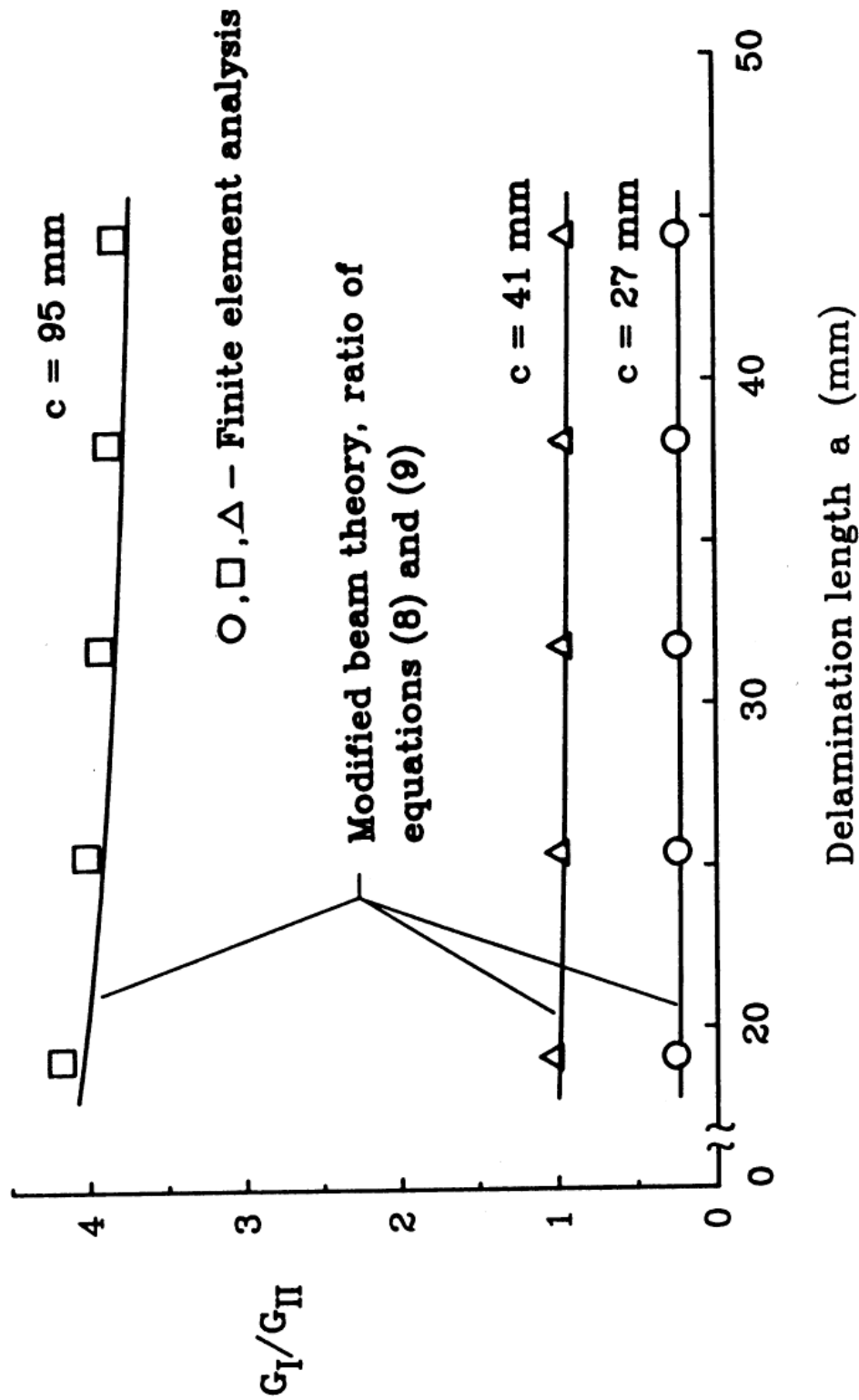


Figure 16. - Comparison of G_I/G_{II} results.

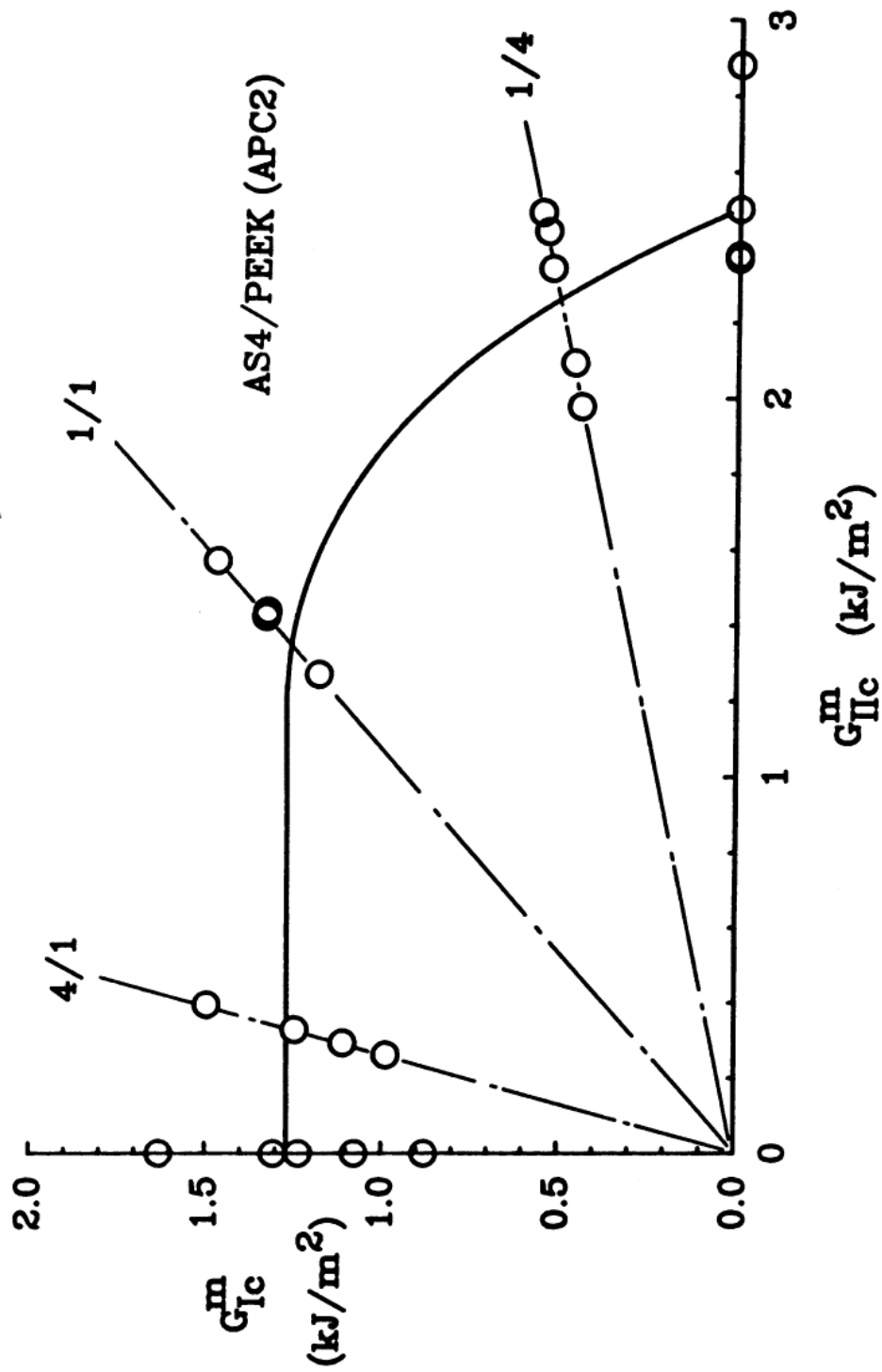


Figure 17. – Delamination toughness measurements from the mixed-mode bending test.



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16. Abstract A mixed-mode delamination test procedure was developed combining double cantilever beam (DCB) mode I loading and end notch flexure (ENF) mode II loading on a split unidirectional laminate. By loading the specimen with a lever, a single applied load simultaneously produces mode I and mode II bending loads on the specimen. This mixed-mode bending (MMB) test was analyzed using both finite element procedures and beam theory to calculate the mode I and mode II components of strain energy release rate, G_I and G_{II} , respectively. The analyses showed that a wide range of G_I/G_{II} ratios could be produced by varying the applied load position on the loading lever. As the delamination extended, the G_I/G_{II} ratios varied by less than five percent. The simple beam theory equations were modified to account for the elastic interaction between the two arms of the specimen and to account for shear deformations. The resulting equations agreed closely with the finite element results and provide a basis for selection of G_I/G_{II} test ratios and a basis for computing the mode I and mode II components of measured delamination toughness. The MMB specimen analysis and test procedures were demonstrated using AS4/PEEK (APC2) unidirectional laminates.			
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